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SECURE CRYPTOSYSTEM BASED ON BRAIDING/ENTANGLEMENT OF PAULI 5/2 MATRICES

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Abstract

Cryptography is the art or science encompassing the principles and methods of transforming an intelligible message into one that is unintelligible and then retransforming that message back to its original form. Secure transmission of the information to the genuine recipient has become a Herculean task .This paper presents a novel encryption scheme using Braiding/Entanglement of Pauli Spin 5/2 matrices.

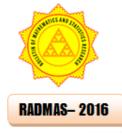
Key Words: Braiding/Entanglement, Encryption and Decryption.

1. INTRODUCTION

The Hill cipher was invented in 1929 by Lester S. Hill [1]. based on matrix transformation that its attributes, including its cryptanalysis are described in some cryptographic textbooks [3]. The Hill cipher was invented in 1929 by Lester S. Hill [1,2]. It is a famous polygram and classical ciphering algorithm based on matrix transformation that its attributes, including its cryptanalysis are described in some cryptographic textbooks [3,4]. It is a famous Polygram and classical ciphering algorithm based on matrix transformation. Hill cipher is a blockcipher having diverse advantages such as concealing letter frequency, its simplicity because of using matrix multiplication and inversion for encryption and decryption and high speed. But it is vulnerable to known plain text attacks. Several researchers tried to improve the security of the Hill cipher. The present paper describes a novel encryption algorithm using braiding/entanglement technique with Pauli 5/2 matrices.

1.1 Pauli Spin 5/2 Matrices:

In Quantum Mechanics a very class of dynamical problems arises with central forces. These forces are derivable from a potential that depends on the distance (r) of the moving particle from a fixed point, the origin of the co-ordinate system (O). Since central forces produce no torque about the origin, the angular momentum L = rxp is constant of motion where p is a constant of motion the momentum of the particle. In addition to the dynamical variables x,y,z to describe the position of the vector there is another fourth variable σ , called the spin angular momentum variable required to describe the dynamical state of fundamental particles. In 1920's, in the study of the spectra of alkali atoms, some troublesome features were observed which could not be explained on the basis of orbital quantum properties [2]. The energy levels corresponding to the n, I and mI quantum numbers were found to be further split up. Uhlenbeck and Goudsmit [3,4] in 1925 attributed these difficulties due to the fact that the electron has an additional property of intrinsic angular momentum and magnetic momentum. Pauli was the first to propose a non-relativistic wave equation, which takes into account the intrinsic magnetic moment of the electron. To describe the electron spin he used spin ½, spin 3/2, spin 5/2 matrices. The spin-5/2 matrices are



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$$S_{x} = \frac{1}{2} \begin{bmatrix} 0 & \sqrt{5} & 0 & 0 & 0 & 0 \\ \sqrt{5} & 0 & \sqrt{8} & 0 & 0 & 0 \\ 0 & \sqrt{8} & 0 & \sqrt{9} & 0 & 0 \\ 0 & 0 & \sqrt{9} & 0 & \sqrt{8} & 0 \\ 0 & 0 & 0 & \sqrt{8} & 0 & \sqrt{5} \\ 0 & 0 & 0 & \sqrt{8} & 0 & \sqrt{5} \\ 0 & 0 & 0 & 0 & \sqrt{5} & 0 \end{bmatrix}$$
$$S_{y} = \frac{1}{2i} \begin{bmatrix} 0 & \sqrt{5} & 0 & 0 & 0 & 0 \\ -\sqrt{5} & 0 & \sqrt{8} & 0 & 0 & 0 \\ 0 & -\sqrt{8} & 0 & \sqrt{9} & 0 & 0 \\ 0 & 0 & -\sqrt{9} & 0 & \sqrt{8} & 0 \\ 0 & 0 & 0 & -\sqrt{8} & 0 & \sqrt{5} \\ 0 & 0 & 0 & -\sqrt{5} & 0 \end{bmatrix}$$
$$S_{z} = \frac{1}{2} \begin{bmatrix} 5 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & -3 & 0 \\ 0 & 0 & 0 & 0 & 0 & -5 \end{bmatrix}$$

1.2 Braiding/Entanglement of Matrices: Entanglement [5] is a term used in quantum theory to describe the way that particles of energy/matter can become correlated to predictably interact with each other regardless of how far apart they are. Braiding/Entanglement of matrices is a technique of generating higher order non-singular matrices from simple lower order non-singular matrices.

For example if a =	<i>a</i> 11	<i>a</i> 12	<i>a</i> 13	$\lceil l$	b 11	b_{12}	b 13		C 11	C 12	C13	$\int d_{11}$	d_{12}	d_{13}
For example if a =	<i>a</i> 21	<i>a</i> 22	a23 , k	=	b ₂₁	b_{22}	<i>b</i> ₂₃	, c =	C21	C 22	<i>c</i> ₂₃ , d :	$= d_{21}$	<i>d</i> 22	<i>d</i> 23
	a 31	<i>a</i> ₃₂	<i>a</i> ₃₃	L	b 31	<i>b</i> ₃₂	b 33		C 31	C 32	C33	d_{31}	<i>d</i> 32	d_{33}

are four non-singular matrices of order 3x3 then these four non-singular matrices are braided/entangled to get higher order 6x6 matrices as

		a_{11}	$a_{_{12}}$	$a_{_{13}}$	b_{11}	b_{12}	<i>b</i> 13	
		<i>a</i> 21	<i>a</i> 22	<i>a</i> 23	b_{21}	b_{22}	<i>b</i> ₂₃	
$A = \begin{bmatrix} a & b \\ c & c \end{bmatrix}$	6]_[a_{31}	<i>a</i> 32	<i>a</i> 33	b_{31}	<i>b</i> ₃₂	<i>b</i> ₃₃	
$\begin{bmatrix} c & c \end{bmatrix}$	$l \rfloor -$	d_{11}	<i>d</i> 12	<i>d</i> ₁₃	C 11	C 12	C 13	
		d_{21}	<i>d</i> 22	<i>d</i> 23	C 21	C 22	C 23	
		<i>d</i> 31	<i>d</i> 32	<i>d</i> 33	C 31	C 32	C33	

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$$B = \begin{bmatrix} c & a \\ b & d \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & d_{11} & d_{12} & d_{13} \\ c_{21} & c_{22} & c_{23} & d_{21} & d_{22} & d_{23} \\ c_{31} & c_{32} & c_{33} & d_{31} & d_{32} & d_{33} \\ b_{11} & b_{12} & b_{13} & a_{11} & a_{12} & a_{13} \\ b_{21} & b_{22} & b_{23} & a_{21} & a_{22} & a_{23} \\ b_{31} & b_{32} & b_{33} & a_{31} & a_{32} & a_{33} \end{bmatrix}$$
$$C = \begin{bmatrix} b & c \\ a & d \end{bmatrix} = \begin{bmatrix} b_{11} & b_{12} & b_{13} & c_{11} & c_{12} & c_{13} \\ b_{21} & b_{22} & b_{23} & c_{21} & c_{22} & c_{23} \\ b_{31} & b_{32} & b_{33} & c_{31} & c_{32} & c_{33} \\ a_{11} & a_{12} & a_{13} & d_{11} & d_{12} & d_{13} \\ a_{21} & a_{22} & a_{23} & d_{21} & d_{22} & d_{23} \\ a_{31} & a_{32} & a_{33} & d_{31} & d_{32} & d_{33} \end{bmatrix}$$

$$D = \begin{bmatrix} c & b \\ a & d \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} & b_{11} & b_{12} & b_{13} \\ c_{21} & c_{22} & c_{23} & b_{21} & b_{22} & b_{23} \\ c_{31} & c_{32} & c_{33} & b_{31} & b_{32} & b_{33} \\ a_{11} & a_{12} & a_{13} & d_{11} & d_{12} & d_{13} \\ a_{21} & a_{22} & a_{23} & d_{21} & d_{22} & d_{23} \\ a_{31} & a_{32} & a_{33} & d_{31} & d_{32} & d_{33} \end{bmatrix}$$

and so on.

В

These matrices are further braided /entangled to get higher order 16x16 matrices like

Α $D \rfloor$ and so on. Non-Singular matrices from the set of these matrices can be selected for |C|the process of encryption/decryption.

1.3 Literature on Golden Matrices: In the last decades the theory of Fibonacci numbers [6,7] was complemented by the theory of the so-called Fibonacci Q – matrix. Stakhov [8] developed a theory

of the golden matrices that are a generalization of the matrix \mathbf{Q}^n for continuous domain. He defined the golden matrices in the terms of the symmetrical hyperbolic Fibonacci functions. B.Vellainkann et.al. [9] used non-singular diagonal matrices of higher order, especially induced from quadratic forms in their encryption algorithm. Bibhudendra Acharya et.al. [10] used Hill Cipher for image encryption. Birendra Goswami [11]used matrices in cloud computing. Ayan Mahalanobis [12] used matrices in public key cryptography.

2. Proposed Method: The set of Pauli Spin 5/2 matrices with some elementary transformations are reduced to the matrices



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	[0	5	0	0	0	0]		0	-5	0	0	0	0
	5	0	8	0	0	0		5	0	-8	0	0	0
h -	0	8	0	9	0	0	c –	0	8	0	-9	0	0
b =	0	0	9	0	8	0	C =	0	0	9	0	-8	0
	0	0	0	8	0	5		0	0	0	8	0	-5
	0	0	0	0	5	0		0	0	0	0	5	0
	$d = \begin{bmatrix} 5 & 0 \\ 0 & 3 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$		0	0	0	(C [C						
	0	3	0	0	0	(0						
d =	0	0	1	0	0	(0						
u –	0	0	0	-1	0	(0						
	0	0	0	0	-3	(0						
	0	0	0	0	0	_	-5						

These three matrices derived from Pauli spin 5/2 matrices along with the identity matrix (1 6x6 = a) are braided or entangled in different possible ways to get a set B of 12nonsingular matrices.

And similarly other matrices are
$$B_{002} = \begin{bmatrix} a & b \\ d & c \end{bmatrix}$$
, $B_{003} = \begin{bmatrix} a & c \\ b & d \end{bmatrix}$, $B_{004} = \begin{bmatrix} a & c \\ d & b \end{bmatrix}$
 $B_{005} = \begin{bmatrix} b & a \\ c & d \end{bmatrix}$, $B_{006} = \begin{bmatrix} b & a \\ d & c \end{bmatrix}$, $B_{007} = \begin{bmatrix} b & d \\ a & c \end{bmatrix}$, $B_{008} = \begin{bmatrix} c & a \\ d & b \end{bmatrix}$, $B_{009} = \begin{bmatrix} c & b \\ a & d \end{bmatrix}$, $B_{010} = \begin{bmatrix} c & d \\ a & b \end{bmatrix}$, $B_{011} = \begin{bmatrix} d & b \\ c & a \end{bmatrix}$, $B_{012} = \begin{bmatrix} d & c \\ b & a \end{bmatrix}$

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2.1. Encryption:

Step 1:The text message is divided into data blocks of 144 characters each. All the 144 characters are coded to decimal equivalents using ASCII table and are written as 12x12 matrix called the message matrix M.

Step 2: Any two matrices say B_{Imn} and B_{opq} from the set B are selected at random. Then the product of these two matrices raised to the powers rst, uvwis computed which is represented as the encoding matrix A.

$A = B_{lmn}^{rst} * B_{opq}^{uvw}$

The Subscript Imn of the first matrix, the power rst to which it is raised and the subscript opq of the second matrix, the power uvw to which it is raised [I m n r s t o p q u v w] successivelyconstitute the secret key. The Alice also encrypts the secret key and communicates to the receiver in a public channel.

Step 3:The message matrix M is multiplied with the encoded matrix A raised to the power't' and the resulting matrix is adjusted to mod 256 called the cipher matrix C.

E= MxA then it is adjusted to mod 256

C = mod (E, 256)

Step 4: All the elements of the matrix C along with the power 1 are coded to the text characters using the ASCII code table which is the cipher text C.

The integer parts of the matrix E when adjusted to mod 256 is named as the integer matrix I.

Example: when 1,209 is adjusted to mod 256 the integer part is 4 and the residue part is 185.

All the elements of the integer matrix I along with the power to which the matrix A is raised are written successively as a string of numbers called the cipher string I.The cipher text C along with the cipher string I are communicated to the Bob in a public channel.

2.2 Encryption of the secret key:

Before communicating the message, the Alice and the Bob agree upon to use a non-singular 12x12matrix S to encrypt and decrypt the secret key. The secret key[I m n r s t o p q u v w] is first converted to weighted 8421 BCD code. The 8421 BCD code thus obtained is gray coded. Then it is 8421BCD decoded and written as 1×12 matrix. This 1×12 matrix is multiplied with the 12x12 matrix S which is already agreed by both the Alice and the BobSaythe 1x12matrix K_E. This K_E is the encrypted secret key and it is sent in public channel to the Bob.

2.3. Decryption:

TheBob after receiving the cipher text C, cipher string I and the encrypted secret key K_E first verifies that the corresponding numeral of the last character of the cipher text C is same as the last numeral in the string I.

2.4 Decryption of the secret key:

To obtain the secret key K from the encrypted key K_E the receiver multiplies the 1x12 matrix K_E with the inverse of the agreed upon 12x12matrix S. Then the elements of the resulting 1x12 matrix are 8421BCD encoded and gray decoded. Finally the result is 8421 BCD decoded to get secret key K. Using the secret key [I m n r s t o p q u v w] the receiver computes the encoding matrix A.

 $A = B_{lmn}^{rst} * B_{opq}^{uvw}$



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Step 1: All the characters of the cipher text C are coded to the decimal equivalentsusing ASCII code table excluding the last numeral and are written as 12x12 matrix say the cipher matrix C. All the elements of the cipher sting I of integers received along with the cipher text C excluding the last numeral are arranged in the form of 12x12 matrix I.

Step 2: Each element of the matrix I is multiplied with 256 and added to the corresponding element of cipher matrix C.

D = 276*I + C (or) Dij= 256lij + Cij

where Dij, lij and Cij are the elements of matrices D, I and C respectively.

Step 3: The matrix D is multiplied with inverse of the encoding matrix A raised to the power t to get the message matrix M.

 $M = D^*[inv (A)]^t$

Step 4:Then the numerals are coded to the text characters using ASCII code table which is the original message.

3.Example: Suppose Alice and Bob want to communicate with each other first they agree upon to use a non-singular 8x8 matrix S for encryption and decryption of the secret key.

	5	2	5	3	7	8	4	1	3	2	6	5]	
	8	9	6	1	7	5	4	2	3	8	9	7	
	8	1	2	6	3	9	5	4	3	2	9	6	
	1	3	5	4	3	9	8	7	6	5	4	3	
	2	1	7	6	8	5	9	4	2	1	2	3	
S=	6	5	7	9	8	9	5	7	2	2	3	9	
3 -	6	7	8	9	4	5	2	1	6	4	9	8	
	7	6	4	3	5	2	1	9	8	1	2	3	
	4	7	6	8	5	5	4	3	2	9	8	3	
	5	3	2	9	6	7	4	3	5	3	2	9	
	5	0	3	5	6	1	7	4	3	5	2	1	
	3	5	2	3	4	3	6	7	8	9	1	3	

3.1. Encryption:

Step 1: Suppose Alice wants to send the message **DONT JUST WAIT FOR GOOD THINGS TO HAPPEN TO YOU WORK HARD TO ACHIEVE YOUR GOAL** to Bob. She converts this message to decimal equivalents using ASCII code table. The text message in the present example has 79 characters. The remaining characters are filled at random. These decimal numbers are arranged in the form of 12x12 matrix M



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	68	79	78	84	32	74	85	83	84	32	87	65	
	73	84	32	70	79	82	32	71	79	79	68	32	
	84	72	73	78	71	83	32	84	79	32	72	65	
	80	80	69	78	32	84	79	32	89	79	85	32	
	87	79	82	75	32	72	65	82	68	32	84	79	
M =	32	65	67	72	73	69	86	69	32	89	79	85	
101 -	82	32	71	79	65	76	83	42	42	42	42	42	
	42	42	42	42	42	42	42	42	42	42	42	42	
	42	42	42	42	42	42	42	42	42	42	42	42	
	42	42	42	42	42	42	42	42	42	42	42	42	
	42	42	42	42	42	42	42	42	42	42	42	42	
	42	42	42	42	42	42	42	42	42	42	42	42	

Step 2:Two matrices B_{01} and B_{04} are selected at random from the set B of matrices. The product of these two matrices B_{01} and B_{04} are raised to the power 01 and is the encoding matrix A.

	[1]	15	0	0	0	0	25	-5	-40	0	0	0]
	25	1	8	0	0	0	5	39	-8	-72	0	0
$A = B_{001}^{001} * B_{004}^{001} =$	0	24	1	-9	0	0	40	8	17	-9	-72	0
	0	0	9	1	-24	0	0	72	9	-17	-8	-40
	0	0	0	-8	1	-25	0	0	72	8	-39	-5
	0	0	0	0	-15	1	0	0	0	40	-39	-5
	25	-5	0	0	0	0	25	-25	40	0	0	0
	5	9	-8	0	0	0	15	-89	-24	72	0	0
	0	8	1	-9	0	0	40	8	-145	-9	72	0
	0	0	9	1	-8	0	0	72	-9	-145	8	40
	0	0	0	8	9	-5	0	0	72	-24	-89	15
	0	0	0	0	5	25	0	0	0	40	-25	-25

The subscripts of these matrices along with the powers [00 100 4 0 0 1 0 0 1] constitute the secret key K.

Step 3: The message matrix M is multiplied with the encoding matrix A raised to the power 1. $E=M^*A^1$ and E is adjusted to mod 256



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	231	125	150	122	62	208	169	61	78	74	82	142]	
	0	242	20	86	125	103	102	240	184	244	53	31	
	32	216	22	30	231	85	104	176	176	82	105	173	
	119	213	163	183	9	171	167	225	99	45	79	191	
	1	213	65	197	95	59	161	67	121	47	245	117	
$C = mod(E_{2}E6) =$	56	40	236	86	38	230	78	68	106	100	74	54	
C= mod (E, 256) =	95	193	98	200	97	59	219	33	138	86	129	211	
	48	136	72	96	192	88	156	32	96	248	128	184	
	48	136	72	96	192	88	156	32	96	248	128	184	
	48	136	72	96	192	88	156	32	96	248	128	184	
	48	136	72	96	192	88	156	32	96	248	128	184	
	48	136	72	96	192	88	156	32	96	248	128	184	

Step 4: All the elements of the matrix C along with the power 1

are coded to the text characters using the ASCII code table which is the cipher text C.

ç}z>Щ=NJRŽ(NULLCHARACTER)òDC4V}gfð_ô5US(SPACE)ØSYNRSçUh°°Ri-wÕ£·HT«§ác-

O¿SOHÕAÅ_;jCy/õu8(ìV&æNDjdJ6_ÁbÈa;

Û!ŠVűÓ0^H`Xœ(SPACE)`ø€,0^H`Xœ(SPACE)`

This cipher text C along with the cipher string I whose last number is 1 is communicated to Bob in a public channel.

3.2Encryption of the secret key: Before communicating the messages Alice and Bob agree upon to use the 12x12nonsingular matrix S.

 $\mathsf{K} = [0\ 0 \ 1 \ 0 \ 0 \ 1 \ 00 \ 4 \ 0 \ 0 \ 1]$

K is 8421BCD encoded to get K_1 .

K₁= [0000 0000 0001 0000 0000 0001 0000 0004 0001]

 K_1 is gray coded to get K_2

K₂= [0000 0000 0001 1000 0000 0001 1000 0000 0110 0000 0000 0001]

K₂ is 8421BCD decoded to get K₃

 $K_3 = [0 \ 0 \ 1 \ 8 \ 0 \ 1 \ 8 \ 0 \ 6 \ 0 \ 0 \ 1]$

 K_3 is multiplied with S to get encrypted key K_{E}

$$\begin{split} & \mathsf{K}_{\mathsf{E}} = \mathsf{K}_3 * \mathsf{S} {=} \begin{bmatrix} 97 \ 133 \ 151 & 170 & 101 \ 163120 \ 100121 & 139 & 165 & 124 \end{bmatrix} \\ & \mathsf{K}_{\mathsf{E}} = {=} \begin{bmatrix} 97 \ 133 \ 151 & 170 & 101 \ 163120 \ 100121 & 139 & 165 & 124 \end{bmatrix} \end{split}$$

is sent to Bob as encrypted secret key in a Public channel.

3.3. Decryption:

Before attempting for the decryption Bob verifies that the numeral corresponding to the last character in the cipher text C is same as the last numeral in the cipher string I.Bob starts the decryption process as follows. **Decryption of the secret key**:

K_E = [97 133 151 170 101 163120 100121 139 165 124]

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 $K_3 = KE * Inv(s) = [0 \ 0 \ 1 \ 8 \ 0 \ 1 \ 8 \ 0 \ 6 \ 0 \ 0 \ 1]$

K₃ is 8421 BCD encoded to get K₂

 $K_{\rm 2}$ is gray decoded to get $K_{\rm 1}$

K₁=[0000 0000 0001 0000 0000 0001 0000 0000 0100 0000 0001] Finally it is 8421 BCD decoded to get decrypted key K

$\mathsf{K} = \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 10 & 4 & 0 & 0 & 1 \end{bmatrix}$

Step 1:Using the secret key Bob selects the matrices B_{01} and B_{04} from the set of B of matrices.He computes the product of these two matrices raised to the power 001 and 001 in the correct order.

	1	15	0	0	0	0	25	-5	-40	0	0	0]	
	25	1	8	0	0	0	5	39	-8	-72	0	0	
	0	24	1	-9	0	0	40	8	17	-9	-72	0	
$A = B_{001}^{001} * B_{004}^{001} =$	0	0	9	1	-24	0	0	72	9	-17	-8	-40	
	0	0	0	-8	1	-25	0	0	72	8	-39	-5	
	0	0	0	0	-15	1	0	0	0	40	-39	-5	
	25	-5	0	0	0	0	25	-25	40	0	0	0	
	5	9	-8	0	0	0	15	-89	-24	72	0	0	
	0	8	1	-9	0	0	40	8	-145	-9	72	0	
	0	0	9	1	-8	0	0	72	-9	-145	8	40	
	0	0	0	8	9	-5	0	0	72	-24	-89	15	
	0	0	0	0	5	25	0	0	0	40	-25	-25	

Step 2: The cipher text C excluding the last character is coded to the decimal numbers using ASCII code table and all the numbers are written as 12x12 matrix, the cipher matrix C.

Step 3:The String I of integers received along with the cipher text in public is converting to 8x8 matrix I excluding the last numeral.

D=256*I+C is computed

Step 4:The matrix D is multiplied with the inverse of encoding matrix A raised to the power 1 to get the matrix M.

 $M = D * Inv[A^1]$

73 78 M = 42 42 42 42 42 42 42 42 42 42 42 42 42 42 42

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All the elements are coded to text characters using the ASCII code table which is the original message **DONT JUST WAIT FOR GOOD THINGS TO HAPPEN TO YOU WORK HARD TO ACHIEVE YOUR GOAL 4. Cryptanalysis and Conclusions:**

The original message contains only 79 characters but the size of the block here is 144. So, the remaining characters are dummy which may be selected at random. Here same dummy character "." is selected to fill the remaining characters. But, in the cipher the same character is mapped to different characters. This shields the cipher against the security implications like chosen plain text attacks, chosen cipher text attacks, linear cryptanalysis and mono-alphabetic cryptanalysis. In the proposed algorithm encoding matrix A is the product of two matrices B_{Imn} and B_{opq} belonging to the set B. The size of key space can be increased by braiding the elements of the set B to form 16x16 non-singular matrices of the type

 $\begin{bmatrix} B_{pq} & 0\\ 0 & B_{rs} \end{bmatrix} \operatorname{or} \begin{bmatrix} B_{pq} & B_{rs}\\ 0 & B_{tu} \end{bmatrix} \operatorname{or} \begin{bmatrix} B_{pq} & 0\\ B_{rs} & B_{tu} \end{bmatrix} \operatorname{and} \operatorname{so} \operatorname{on}.$

The encrypted secret key can be decrypted only by the authenticated receiver. i.e., who knows the matrix S. The procedure can be further improved to enhance the security level by selecting more matrices from the set B of matrices and raising each matrix to the power f(i,j) where the function f(i,j) is confidential between the communicating parties. So, the encryption algorithm presented here provides high level of security at relatively low computational overhead.

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